

Q7. If hydrogen atom is bombarded by energetic electrons, it will emit

- (a) K_α X - rays (b) β -rays
(c) Neutrons (d) none of the above

Ans.: (d)

Q8. A hydrogen atom in its ground state is collided with an electron of kinetic energy 13.377 eV. The maximum factor by which the radius of the atom would increase is

- (a) 7 (b) 8 (c) 49 (d) 64

Ans.: (c)

Solution: $E_n = \frac{-13.6}{n^2} eV$

$\Rightarrow E_1 = -13.6 eV, E_2 = -3.4 eV, E_3 = 1.5 eV, E_4 = 0.85 eV, E_5 = 0.54 eV$

$E_6 = 0.3777 eV, E_7 = 0.2775 eV$

Since Electron have kinetic energy $13.377 eV = -13.6 + 0.2775 eV \Rightarrow n = 7$

$\therefore r_n = a_0 n^2 \Rightarrow r_n = 49a_0$

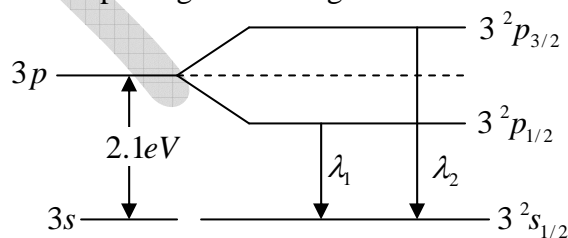
JEST 2015

Q9. The energy difference between the $3p$ and $3s$ levels in Na is $2.1 eV$. Spin-orbit coupling splits the $3p$ level, resulting in two emission lines differing by 6\AA . The splitting of the $3p$ level is approximately,

- (a) $2 eV$ (b) $0.2 eV$ (c) $0.02 eV$ (d) $2 meV$

Ans: (d)

Solution: The fine structure splitting of Na in ground and excited state is



The transition $3^2p_{3/2} \rightarrow 3^2s_{1/2}$ produces photon of wavelength λ_2 and corresponding

photon energy is $E_2 = \frac{12400}{\lambda_2 \left(\text{\AA} \right)} eV$

The transition $3^2p_{1/2} \rightarrow 3^2s_{1/2}$ produces photon of wavelength λ_1 and corresponding photon energy is $E_1 = \frac{12400}{\lambda_1(\text{\AA}^0)} eV$. The separation between $^2p_{3/2}$ and $^2p_{1/2}$ is

$$\Delta E = E_2 - E_1 = \frac{12400}{\lambda_2} - \frac{12400}{\lambda_1} = 12400 \left(\frac{1}{\lambda_2} - \frac{1}{\lambda_1} \right) = 12400 \left(\frac{\lambda_1 - \lambda_2}{\lambda_1 \lambda_2} \right)$$

Given $\Delta\lambda = \lambda_1 - \lambda_2 = 6\text{\AA}^0$ also fine structure splitting is of the order of $10^{-3} eV$.

Thus λ_1 and λ_2 are approximately same as λ corresponds to $3p \rightarrow 3s$, whereas

wavelength (λ) corresponding to $3p \rightarrow 3s$ transition is $\lambda = \frac{12400}{2.1} \text{\AA}^0$

Thus, $\lambda_1 \lambda_2 \cong \lambda^2 = \left(\frac{12400}{2.1} \right)^2$

$$\therefore \Delta E = 12400 \times \frac{6}{\left(\frac{12400}{2.1} \right)^2} = \frac{2.1 \times 2.1 \times 6}{12400} \cong 2 \times 10^{-3} eV \Rightarrow \Delta E = 2 meV$$

Q10. Which of the following excited states of a hydrogen atom has the highest lifetime?

- (a) $2p$ (b) $2s$ (c) $3s$ (d) $3p$

Ans.: (b)

Solution: $2p$ and $3p$ are normal states. Electron from $2p$ and $3p$ make transition to ground state within 10^{-9} sec. Electron in $3s$ state although can not come directly to ground state but it can come to $1s$ through $2p$ as $3s \rightarrow 2p \rightarrow 1s$, while $2s$ is metastable state and electron in $2s$ state can make transition to $1s$ slowly. Thus $2s$ has long life time.

Q11. Which of the following statements is true for the energies of the terms of the carbon atom in the ground state electronic configuration $1s^2 2s^2 2p^2$?

- (a) $^3P < ^1D < ^1S$ (b) $^3P < ^1S < ^1D$
 (c) $^3P < ^1F < ^1S$ (d) $^3P < ^1F < ^1D$

Ans.: (a)

Solution: The spectroscopy terms for p^2 are $^1S_0, ^1D_2, ^3P_2$. According to Hund's rule, state with highest multiplicity lies lowest. Then, out of same multiplicity, state with highest L lies lowest. Thus these terms can be arranged as $^3P < ^1D < ^1S$

JEST 2016

Q12. The H_2 molecule has a reduced mass $M = 8.35 \times 10^{-28} \text{ kg}$ and an equilibrium internuclear distance $R = 0.742 \times 10^{-10} \text{ m}$. The rotational energy in terms of the rotational quantum number J is

- (a) $E_{rot}(J) = 7J(J-1) \text{ meV}$ (b) $E_{rot}(J) = \frac{5}{2}J(J+1) \text{ meV}$
 (c) $E_{rot}(J) = 7J(J+1) \text{ meV}$ (d) $E_{rot}(J) = \frac{5}{2}J(J-1) \text{ meV}$

Ans. : (c)

Solution: $E = \frac{\hbar^2}{2I} J(J+1)$,

where, $I = \mu r^2 = 8.35 \times 10^{-28} \text{ kg} \times (0.742 \times 10^{-10} \text{ m})^2 = 4.597 \times 10^{-48} \text{ kgm}^2$

$$\therefore \frac{\hbar^2}{2I} = \frac{(1.05 \times 10^{-34} \text{ J}\cdot\text{s})^2}{2 \times (4.597 \times 10^{-48} \text{ kgm}^2)} = \frac{1.112 \times 10^{-68}}{9.18 \times 10^{-48}}$$

$$= 1.21 \times 10^{-21} \text{ J} = 1.21 \times 10^{-21} \times \frac{1}{1.6 \times 10^{-19}} \text{ eV} = 7.57 \times 10^{-3} \text{ eV} = 7.57 \text{ meV}$$

$\therefore E \cong 7J(J+1) \text{ meV}$

Q13. If the Rydberg constant of an atom of finite nuclear mass is αR_∞ , where R_∞ the Rydberg constant corresponding to an infinite nuclear mass, the ratio of the electronic to nuclear mass of the atom is:-

- (a) $\frac{(1-\alpha)}{\alpha}$ (b) $\frac{(\alpha-1)}{\alpha}$ (c) $(1-\alpha)$ (d) $\frac{1}{\alpha}$

Ans. : (a)

Solution: $R_M = \frac{R_\infty}{1 + \frac{m_c}{M}} \Rightarrow \alpha = \frac{1}{1 + \frac{m_c}{M}} \Rightarrow 1 + \frac{m_c}{M} = \frac{1}{\alpha} \Rightarrow \frac{m_c}{M} = \frac{1}{\alpha} - 1 = \frac{1-\alpha}{\alpha}$