



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

### GS-2011 (Physics)

#### TATA INSTITUTE OF FUNDAMENTAL RESEARCH

Written Test in **PHYSICS** - December 12, 2010

Duration: Three hours (3 hours)

Name:	Ref. Code:
Tume:	11c1. Code

#### Please read all instructions carefully before you attempt the questions.

- 1. Please fill-in details about name, reference code etc. on the question paper and answer sheet. The Answer Sheet is machine-readable. Read the instructions given on the reverse of the answer sheet before you start filling it up. Use only HB pencils to fill-in the answer sheet.
- 2. Indicate your ANSWER ON THE ANSWER SHEET by blackening the appropriate circle for each question. *Do not mark more than one circle for any question*: this will be treated as a wrong answer.
- 3. This test comes in two sections, **Section A** and **Section B**, both of which contain multiple choice-type questions. Only ONE of the options given at the end of each question is correct. Section A contains 20 questions, each with 4 options, and Section B contains 8 questions, each with 6 options. The maximum marks are 60 for Section A plus 40 for Section B, totaling to 100. Marking shall be as follows:
- (i) If the answer is **correct**: +3 marks in Section A; +4 marks in Section B
- (ii) If the answer is incorrect: -1 mark in both Section A & B
- (iii) If the answer is **not attempted**: 0 marks in both Section A & B
- (iv) If more than one box is **marked**: 0 marks in both Section A & B Note that negative marking as indicated above will be implemented.

Email: fiziks.physics@gmail.com



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- 4. As a rough guideline, the time spent on questions in Section A should be about 5 minutes each; questions in Section B should take about 10 minutes each. Obviously, some questions may take a little less time while others may require a little more.
- 5. We advise you to first mark the correct answers on the QUESTION PAPER and then to TRANSFER these to the ANSWER SHEET only when you are sure of your choice.
- 6. Rough work may be done on blank pages of the question paper. If needed, you may ask for extra rough sheets from an Invigilator.
- 7. **Use of calculators is permitted**. Calculator which plots graphs is NOT allowed. Multiple-use devices such as cell phones, smart phones etc., CANNOT be used for this purpose.
- 8. Do NOT ask for clarifications from the invigilators regarding the questions. They have been instructed not to respond to any such inquiries from candidates. In case a Correction/clarification is deemed necessary; the invigilator(s) will announce it publicly.



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### GS-2011 (Physics)

A SECTION: 20 x 3= 60 Marks

Q.1 The infinite series

$$x + \frac{x^3}{3} + \frac{x^5}{5} + \frac{x^7}{7} + \dots$$

where -1 < x < +1, can be summed to the value

(a) 
$$\frac{1}{2} \ln[(1+x)/(1-x)]$$

(b) 
$$\frac{1}{2} \ln[(1-x)/(1+x)]$$

(c) tanhx

(d) 
$$\ln\left(1-\frac{4}{\pi}\tan^{-1}x\right)$$

Q.2 A 100 page book is known to have 200 printing errors distributed randomly through the pages. The probability that one of the pages will be found to be completely free of errors is closest to

(a) 13%

- (b) 25%
- (c) 50%

(d) 67%

Q.3 Consider the matrix

$$M = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix}$$

A 3-dimensional basis formed by eigenvectors of M is

(a)  $\begin{pmatrix} 2 \\ 1 \\ -1 \end{pmatrix}$ ,  $\begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$ 

(b)  $\begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$ ,  $\begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$ 

(c)  $\begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}$ ,  $\begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}$ 

- (d)  $\begin{pmatrix} 2 \\ 1 \\ -1 \end{pmatrix}$ ,  $\begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$  and  $\begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix}$
- Q.4 Two solid spheres  $S_1$  and  $S_2$  of the same uniform density fall from rest under gravity in a viscous medium and, after some time, reach terminal velocities  $v_1$  and  $v_2$  respectively. If the masses of  $S_1$  and  $S_2$  are  $m_1$  and  $m_2$  respectively, and  $v_1 = 4v_2$ , then the ratio  $m_1 / m_2$  is
  - (a) 1/8

(b) 8

 $(c) \frac{1}{4}$ 

(d) 4



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Q.5 The dynamics of a particle of mass m is described in terms of three generalized coordinates  $\zeta$ ,  $\eta$  and  $\varphi$ . If the Lagrangian of the system is

$$L = \frac{1}{8} m \left[ (\zeta + \eta) \left( \frac{\dot{\zeta}^{2}}{\zeta^{2}} + \frac{\dot{\eta}^{2}}{\eta^{2}} \right) + 4\zeta \eta \dot{\phi}^{2} \right] + \frac{1}{8} k (\zeta + \eta)^{2}$$

where k is a constant, then a conserved quantity in the system will be

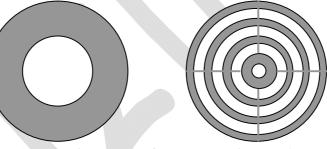
(a) 
$$(m+k)(\dot{\zeta}+\dot{\eta})$$

(b) 
$$m(\zeta + \eta)(\dot{\zeta}/\zeta^2 + \dot{\eta}/\eta^2)$$

(c) 
$$m(\dot{\zeta}^2/\eta^2 + \dot{\eta}^2/\zeta^2)$$

(d) 
$$m\zeta\eta\dot{\phi}$$

Q.6 A scientist is given two heavy spheres made of the same metal, which have the same diameter and weight, and is asked to distinguish the spheres, without damaging them in any way. Though the spheres look identical, one of them is actually a hallow spherical shell, while the other is a set of concentric shells mounted on four thin rods of the same metal (see figure).



To make this distinction, the scientist must perform an experiment where each sphere is

- (a) immersed fully in a non-corrosive liquid and then weighed
- (b) made into the bob of a long simple pendulum and set oscillating
- (c) set rotating under the action of a constant torque
- (d) given the same electric charge Q and the potential is measured
- Q.7 A narrow beam of light of wavelength 589.3 *nm* from a sodium lamp is incident normally on a diffraction grating of transmission type. If the grating constant is 1000000 m<sup>-1</sup> the number of principal maxima observed in the transmitted light will be
  - (a) 1

(b) 3

(c)5

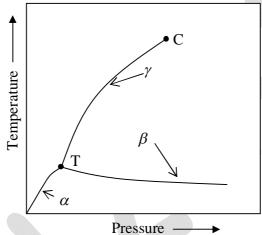
(d)7



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- Q.8 A closed, thermally-insulated box contains one mole of an ideal monatomic gas G in thermodynamic equilibrium with blackbody radiation B. The total internal energy of the system is  $U = U_G + U_B$  where  $U_G$  and  $U_B$  ( $\propto T^4$ ) are the energies of the ideal gas and the radiation respectively. If  $U_G = U_B$  at the temperature  $T_0$  K, then the energy required to raise the temperature from  $T_0$  K to ( $T_0 + 1$ ) K, in terms of the gas constant R, is
  - (a) 0.33R

- (b) 1.5 R
- (c) 6R
- (d) 7.5R
- Q.9 The phase diagram of a pure substance is given in the figure below, where 'T' denotes the triple point and 'C' denotes the critical point.



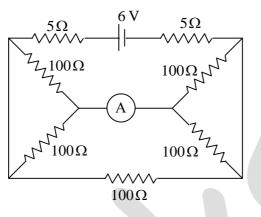
The phase transitions occurring along the lines marked  $\alpha$ ,  $\beta$  and  $\gamma$  are

- (a)  $\alpha$  = melting;  $\beta$  = condensation;  $\gamma$  = sublimation
- (b)  $\alpha$  = sublimation;  $\beta$  = vaporisation;  $\gamma$  = melting
- (c)  $\alpha$  = melting;  $\beta$  = vaporisation;  $\gamma$  = condensation
- (d)  $\alpha$  = sublimation;  $\beta$  = melting;  $\gamma$  = vaporisation



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Q.10 The current read by the ammeter (A) in the circuit given below is



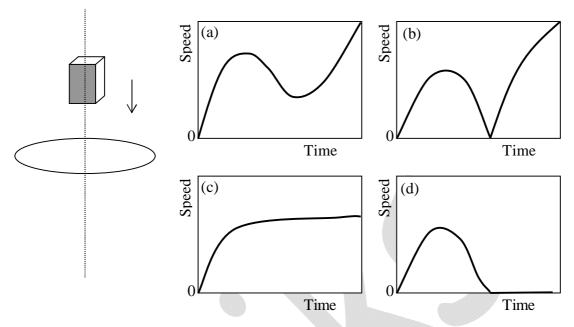
- (a) 50.0 mA
- (b) 100.0 mA
- (c) 27.3 mA
- (d) 54.5 mA

6

- Q.11 The sign of the majority charge carries in a doped silicon crystal is to be determined experimentally. In addition to a voltage supply the combination of instruments needed to perform the experiment is
  - (a) Thermometer, Voltmeter and Ammeter
  - (b) Magnet, Voltmeter and Ammeter
  - (c) pickup Coil, Voltmeter and Ammeter
  - (d) Heater, Magnet and Thermometer
- Q.12 A small but very powerful bar magnet falls from rest under gravity through the centre of a horizontal ring of conducting wire, as shown in the figure below (on the left). The speed-versus-time graph, in arbitrary units of the magnet will correspond most closely to which of the four plots below (on the right)?



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- Q.13 The spectra of electromagnetic radiation emitted by distant objects like stars and galaxies give important clues about their physical properties. In this context, a correct statement is that
  - (a) the wavelengths in the emission spectrum of an element in a star are always the same as those found in laboratory experiments
  - (b) absorption spectra cannot be used to determine which molecules are present in the distant objects
  - (c) the nuclear structure of the distant objects cannot be determined from lines in the visible region of the spectrum
  - (d) absorption lines in the spectra of distant objects do not carry information about their motion in a direction transverse to the line of sight
- Q14 Given that the ionization energies of Hydrogen ( ${}^{1}H$ ) and Lithium ( ${}^{3}Li$ ) are 13.6 eV and 5.39 eV, respectively, the effective nuclear charge experience by the valence electron of a  ${}^{3}Li$  atom may be estimated in terms of the proton charge e as
  - (a) 3.00 e
- (b) 1.59 *e*
- (c) 1.26 *e*
- (d) 0.63 e



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- Q.15 Two identical non-interacting particles, each of mass m and spin  $\frac{1}{2}$ , are placed in a one-dimensional box of length L. In quantum mechanics, the lowest possible value of the total energy of these two particles is  $\varepsilon_0$ . If instead, four such particles are introduced into a similar one-dimensional box of length 2L, then the lowest possible value of their total energy will be
  - (a)  $\varepsilon_0$

- (b)  $\frac{5\varepsilon_0}{4}$
- (c)  $3\varepsilon_0/4$
- (d)  $2\varepsilon_0$

Q.16 An excited atomic electron undergoes a spontaneous transition

$$3d_{3/2} \rightarrow 2p_{1/2}$$

The interaction responsible for this transition must be of the type

- (a) electric dipole (E1)
- OR magnetic dipole (M1)
- (b) electric quadrupole (E2)
  - OR magnetic dipole (M1)
- (c) electric quadrupole (E2) OR
- magnetic quadrupole (M2)
- (d) electric dipole (E1)
- OR magnetic quadrupole (M2)
- Q.17 A fast-moving  $^{14}N$  nucleus collides with an  $\alpha$  particle at rest in the laboratory frame, giving rise to the reaction

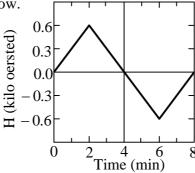
$$^{14}N + \alpha \rightarrow ^{17}O + p$$

Given the masses 14.00307 a.m.u and 16.99913 a.m.u. for  $^{14}N$  and  $^{17}O$  nuclei respectively, and 4.00260 a.m.u. and 1.00783 a.m.u. for  $\alpha$  and p respectively, the minimum kinetic energy in the laboratory frame of the  $^{14}N$  nucleus must be

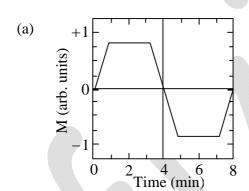
- (a) 1.20 *MeV*
- (b) 1.55 *MeV*
- (c) 4.20 *MeV*
- (d) 5.41 MeV

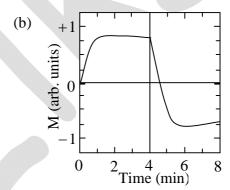
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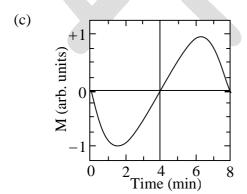
Q.18 An unmagnetised sample of iron is placed in a magnetic field H which varies with time as shown in the plot below.

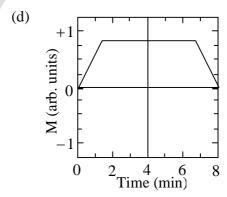


The magnetization M of the iron sample is continuously measured and also plotted as a function of time. The appearance of this plot will be closest to







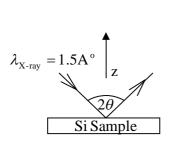


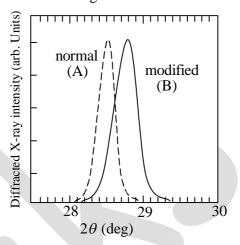
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Q.19 The figure below shows the Bragg diffraction pattern for *X*-rays of wavelength 1.54 Å incident on two crystalline Silicon thin film Sample A and B. The dashed line corresponds to a normal Sample A and the continuous line corresponds to another Sample B, which is modified due to differences in the growth conditions.





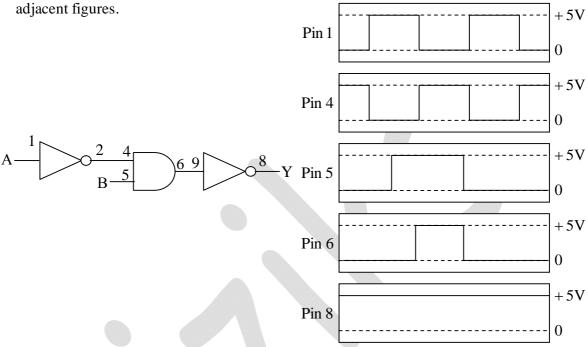
These plots suggest that the modified sample B is

- (a) stretched in all direction by 3%
- (b) compressed in all directions by 3%
- (c) stretched in the z direction by 1% and possibly compressed in x and y directions
- (d) compressed in the z direction by 1% and possibly stretched out in x and y directions



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Q.20 The digital electronic circuit shown below (left side) has some problem and is not performing as intended. The voltage at each pin as a function of time is shown in the



The problem in the about circuit may be that

(a) the Pin 8 is clamped to +5

- (b) the input inverter is shorted
- (c) the Pin 6 is shorted to ground
- (d) OR gate is used instead of AND gate

### GS-2011 (PHYSICS)

**PART-B** (MARKS: 8 x 5=40)

Q.1 The trace of the real 4 x 4 matrix U = exp(A), where

$$A = \begin{pmatrix} 0 & 0 & 0 & \pi/4 \\ 0 & 0 & -\pi/4 & 0 \\ 0 & \pi/4 & 0 & 0 \\ -\pi/4 & 0 & 0 & 0 \end{pmatrix}$$
 is equal to

(a) 2

(b)  $\pi/4$ 

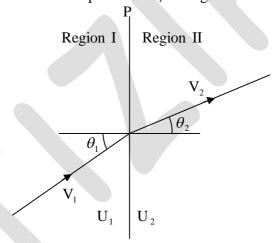
(c)  $exp(i\varphi)$  for  $\varphi = 0, \pi$ 

(d) zero

(e)  $\pi/2$ 

(f)  $2\sqrt{2}$ 

Q.2 A region of space is divided into two parts by a plane P, as shown in the figure below. A particle of mass m passes from Region I and Region II where it has speed  $v_1$  and  $v_2$ respectively. There is a constant potential U<sub>1</sub> in Region I and U<sub>2</sub> in Region II.



Let T<sub>1</sub> be the kinetic energy of the particle in Region I. If the trajectory of the particle is inclined to the normal to the plane P by angles  $\theta_1$  and  $\theta_2$ , as shown in the figure then the ratio  $\sin \theta_1 / \sin \theta_2$  is given by

- (a)  $\sqrt{1-T_1/(U_1-U_2)}$  (b)  $\sqrt{1+T_1/(U_1-U_2)}$  (c)  $\sqrt{1+(U_1-U_2)/T_1}$  (d)  $\sqrt{1+(U_1+U_2)/T_1}$  (e)  $\sqrt{1-T_1(U_1-U_2)}$  (f)  $\sqrt{1-(U_1-U_2)/T_1}$



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Q.3 The electric field of an electromagnetic wave of angular frequency  $\omega$  propagating in a medium with conductivity  $\sigma$ , permittivity  $\varepsilon$  and permeability  $\mu$  is given by

$$E = E_0 \exp[-i(\omega t - kx)]$$

where the imaginary part of the complex propagation constant k is  $\omega\sqrt{\mu\varepsilon/2}$  multiplied by the factor

(a) 
$$\left[ \sqrt{1 + \sqrt{\sigma / \omega \varepsilon}} + 1 \right]^{1/2}$$

(b) 
$$\left[\sqrt{1+\sigma/\omega\varepsilon}+1\right]^{1/2}$$

(c) 
$$\left[\sqrt{1+\left(\sigma/\omega\varepsilon\right)^2}+1\right]^{1/2}$$

(d) 
$$\left[\sqrt{1+\left(\sigma/\omega\varepsilon\right)^2}-1\right]^{1/2}$$

(e) 
$$\left[ \sqrt{1 + \sqrt{\sigma / \omega \varepsilon}} - 1 \right]^{1/2}$$

(f) 
$$\left[\sqrt{1+\sigma/\omega\varepsilon}-1\right]^{1/2}$$

Q.4 A system having N non-degenerate energy eigenstates is populated by N identical spin-zero particles and 2N identical spin-half particles. There are no interactions between any of these particles. If N = 1000, the entropy of the system is closet to

(a) zero

(b)  $1000 k_B$ 

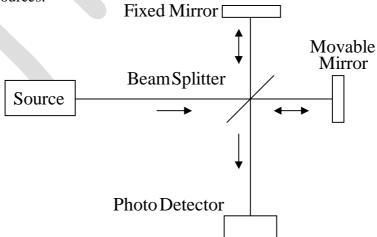
(c)  $13.82 k_B$ 

(d)  $693.1 k_B$ 

(e)  $5909.693 k_B$ 

(f)  $6909 k_B$ 

Q.5 The Michelson interferometer in the figure below can be used to study properties of light emitted by distant sources.





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A Source  $S_1$ , when at rest, is known to emit light of wavelength 632.8 nm. In this case, if the Movable Mirror is translated through a distance d, it is seen that 99,565 interference fringes pass across the Photo-Director. For another source  $S_2$ , moving at an uniform speed of 1.5 x  $10^7 \, ms^{-1}$  towards the interferometer along the straight line joining it to the Beam Splitter, one sees 100,068 interference fringes pass across the Photo-Detector for the same displacement d of the Movable Mirror. It follows that  $S_2$ , in its own rest frame, must be emitting light of wavelength

(a) 599.6 nm

(b) 598.9 nm

(c) 628.0 nm

(d) 631.2 nm

(e) 661.9 nm

- (f) 662.8 nm
- Q.6 A particle of mass m is placed in the ground state of a one-dimensional harmonic oscillator potential of the form

$$V(x) = \frac{1}{2}kx^2$$

where the stiffness constant k can be varied externally. The ground state wavefunction has the form  $\psi(x) \propto \exp(-ax^2\sqrt{k})$  where a is a constant. If, suddenly, the parameter k is changed to 4k, the probability that the particle will remain in the ground state of the new potential is

(a) 0.06

(b) 0.94

(c) 0.53

(d) 0.47

(e) 0.33

- (f) 0.67
- Q.7 A Cloud Chamber of width 0.01 m is filled with pure nitrogen gas  $(N_2)$  at normal temperature and pressure. A beam of  $\alpha$  particles, when incident normally on the chamber, make tracks which are visible under strong illumination. Whenever an  $\alpha$  particle  $^4_2$ He has a nuclear collision with a  $^{14}_7$ N nucleus, the track shows a distinct bend. The radius of a nucleus is given by  $r = r_0 A^{1/3}$  where  $r_0 = 1.27 \times 10^{-5} m$  and A is the atomic mass number. If the  $\alpha$  particles move at non-relativistic speeds and the total number of incident of  $\alpha$  particles is  $10^7$ , the number of such distinct bends is approximately
  - (a) 100

(b) 200

(c) 300

(d)400

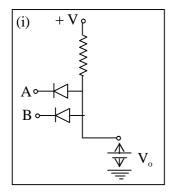
(e) 500

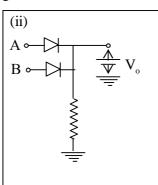
(f) 600

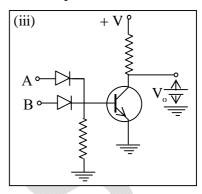


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Q.8 The three electronic circuits marked (i), (ii) and (iii) in the figure below can all work as logic gates, where the input signals are either 0V or 5V and the output is  $V_o$ .







Identify the correct combination of logic gates (i), (ii), (iii) in the options given below.

- (a) AND, OR, NOR
- (b) OR, NAND, NOR
- (c) NAND, AND, XOR

- (d) XOR, AND, NAND
- (e) NOR, XOR, AND
- (f) NOR, NAND, OR

Email: fiziks.physics@gmail.com