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Learn Physics in Right Way



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JEST Physics

Question Paper -2023

Learn Physics in Right Way

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Section A

Correct answer: +3, wrong answer: -1.

Q1. The position and velocity vectors of a particle changes from \vec{R}_1 to \vec{R}_2 and \vec{v}_1 to \vec{v}_2 respectively as time flows from t_1 to t_2 . If $\vec{r}(t)$, $\vec{v}(t)$, and $\vec{a}(t)$ are the instantaneous position, velocity and acceleration vectors of the particle, compute the integral:

$$\vec{I} = \int_{t_1}^{t_2} \vec{r} \times \vec{a} dt$$

Mark the correct answer.

- (a) $\vec{I} = \vec{R}_2 \times \vec{v}_2 - \vec{R}_1 \times \vec{v}_1$ (b) $\vec{I} = \vec{R}_1 \times \vec{v}_1 - \vec{R}_2 \times \vec{v}_2$
 (c) $\vec{I} = 0$ (d) $|\vec{I}| = |\vec{R}_1 \times \vec{v}_1| + |\vec{R}_2 \times \vec{v}_2|$

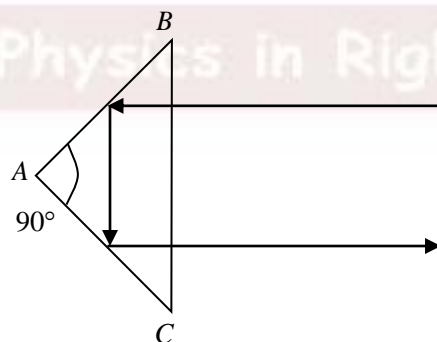
Ans: 1. (a)

Q2. A beam of light is propagating through a block of glass with refractive index n . The block is moving with a constant speed v in the direction opposite to that of the beam. The speed of the light beam in the block as measured by an observer in the laboratory frame is:

- (a) $\frac{c}{2n}$ (b) $\frac{c}{n}$
 (c) $\frac{c}{2n}$ (d) $\frac{c - nv}{n - \frac{v}{c}}$

Ans: 2. (d)

Q3. A right-angled prism is placed in air (the refractive index of air is 1) and a light beam is incident perpendicular to the base of the prism as shown in the figure. In order to get the light beam totally reflected, the minimum value of the refractive index of the prism should be



- (a) 1 (b) $\frac{\sqrt{3}}{2}$ (c) $\frac{\pi}{2}$ (d) $\sqrt{2}$

Ans: 3. (d)

Q4. Consider a spin-1/2 particle in the quantum state

$$|\psi(\beta, \alpha)\rangle = \cos\left(\frac{\beta}{2}\right)|\uparrow\rangle + \sin\left(\frac{\beta}{2}\right)e^{i\alpha}|\downarrow\rangle$$

where $0 \leq \beta \leq \pi$ and $0 \leq \alpha \leq 2\pi$. For which values of (δ, γ) is the state $|\psi(\delta, \gamma)\rangle$ orthogonal to $|\psi(\beta, \alpha)\rangle$?

- (a) $(\pi + \beta, \pi - \alpha)$ (b) $(\pi - \beta, \pi - \alpha)$
 (c) $(\pi + \beta, \pi + \alpha)$ (d) $(\pi - \beta, \pi + \alpha)$

Ans: 4. (d)

Q5. Consider a system of classical non-interacting particles constrained to be in the XY plane subject to the potential:

$$V(x, y) = \frac{1}{2}\alpha(x - y)^2$$

If they are in equilibrium with a thermal bath at temperature T , what is the average energy per particle? The Boltzmann constant is k_B .

- (a) $\frac{5}{2}k_B T$ (b) $\frac{1}{2}k_B T$
 (c) $2k_B T$ (d) $\frac{3}{2}k_B T$

Ans: 5. (d)

Q6. There are three states of energy $E, 0, -E$ available for the population of two identical non-interacting spin less fermions. If they are in equilibrium at temperature T , what is the average energy of the system? The Boltzmann constant is k_B and consider β to be $\frac{1}{k_B T}$.

- (a) 0 (b) $\frac{E(e^{\beta E} - e^{-\beta E})}{1 + e^{-\beta E} + e^{\beta E}}$
 (c) $\frac{E(e^{-\beta E} - e^{\beta E})}{1 + e^{-\beta E} + e^{\beta E}}$ (d) $\frac{E(2e^{-\beta E} + e^{-\beta E} - e^{\beta E} - 2e^{2\beta E})}{2e^{-\beta E} + e^{-\beta E} + 2 + e^{\beta E} + 2e^{2\beta E}}$

Ans: 6. (c)

Q7. Consider a free particle in one dimension described by the wavefunction:

$$\psi(x, t=0) = A \exp \frac{ipx}{\hbar} + B \exp \frac{-ipx}{\hbar}$$

The probability current density corresponding to $\psi(x, t)$ at a later time t is:

- (a) $\frac{p(|A|^2 - |B|^2)}{m} \cos\left(\frac{p^2}{2m\hbar}t\right)$ (b) $\frac{p(|A|^2 - |B|^2)}{m}$
- (c) $\frac{p(|A|^2 + |B|^2)}{m}$ (d) $\frac{p(|A|^2 + |B|^2)}{m} \cos\left(\frac{p^2}{2m\hbar}t\right)$

Ans: 7. (b)

Q8. Consider all possible Boolean logic gates with 2 inputs and one output. How many such gates can be constructed?

- (a) 16 (b) 4 (c) 2 (d) 8

Ans: 8. (a)

Q9. If linearly polarized light is sent through two polarizers, the first at 45° to the original axis of polarization and the second at 90° to the original axis of polarization, what fraction of the original intensity passes through the last polarizer?

- (a) $\frac{1}{2}$ (b) $\frac{1}{4}$ (c) 0 (d) $\frac{1}{8}$

Ans: 9. (b)

Q10. A rocket is moving in free space with speed $\frac{c}{2}$. After a fuel tank is gently detached, the

rocket is found to be moving with a speed $\frac{c}{4}$ with respect to the detached fuel tank. What is the

final speed of the rocket in the original frame of reference?

- (a) $\frac{2}{7}c$ (b) $\frac{2}{3}c$ (c) $\frac{3}{4}c$ (d) $\frac{4}{5}c$

Ans: 10. (b)

Q11. Two identical magnetic dipoles of length ℓ , which are free to rotate, are kept fixed at a distance d ($d \gg \ell$). In their minimum energy configuration, they will orient themselves

- (a) anti-parallel to each other and perpendicular to the line joining them
(b) parallel to each other and aligned to the line joining them
(c) anti-parallel to each other and aligned to the line joining them
(d) parallel to each other and perpendicular to the line joining them

Ans: 11. (b)

Q12. The force experienced by a mass confined to move along the x -axis is of the form $F(x) = -k_1x - k_2x^n$ where x is the displacement of the mass from $x = 0$, k_1 and k_2 are positive constants and n is a positive integer. For small displacements, the motion of the mass remains symmetric about $x = 0$

- (a) when n is any positive integer.
- (b) when n is an odd positive integer
- (c) only when $n = 1$
- (d) when n is an even positive integer

Ans: 12. (b)

Q13. A silicon crystal sample has 50 billion silicon atoms and 5 million free electrons. The silicon crystal is additionally doped with 5 million pentavalent atoms. Assume that the ambient thermal energy is much smaller than the bandgap of silicon. How many free electrons and holes are there inside the silicon crystal?

- (a) Number of electrons is 30 million and number of holes is zero.
- (b) Number of electrons is 10 million and number of holes is zero.
- (c) Number of electrons is 10 million and number of holes is 5 million.
- (d) Number of electrons is 5 million and number of holes is 5 million.

Ans: 13. (b)

Q14. Calculate the contour integral

$$I = \oint_C \frac{\cos^2(z) - z^2}{(z-a)^3} dz$$

where the clockwise contour C is encircling the point $z = a$ in the complex plane.

- (a) $-(\sin 2a + 1)2\pi i$
- (b) $(\cos 2a + 1)2\pi i$
- (c) $-(\cos 2a + 1)2\pi i$
- (d) $(\sin 2a + 1)2\pi i$

Ans: 14. (c)

Q15. What is the 2's complement representation of 11010110?

- (a) 11010101
- (b) 00101001
- (c) 00101010
- (d) 01101011

Ans: 15. (c)

Q16. A quantum particle moving in one dimension is in a state having the wave function

$$\psi(x) = \sinh(\lambda x) \exp\left(\frac{-ax^4 + bx + ipx}{\hbar}\right)$$

where a, b, λ and p are all positive real numbers. What is the expectation value of momentum?

- (a) $\hbar\lambda$ (b) p
(c) b (d) $-p$

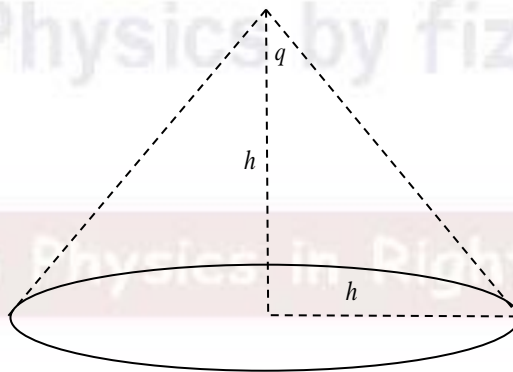
Ans: 16. (b)

Q17. Two particles of mass m and $4m$ confined to move along the x -axis are subjected to the force $F(x) = -kx$. At time $t = 0$, the smaller mass m starts from rest at $x_1(t=0) = A$ and the larger mass $4m$ starts from rest at $x_2(t=0) = -A$. The point on the x -axis where the first collision between the two particles occurs is:

- (a) $x = \frac{A}{2}$ (b) $x = -\frac{A}{2}$
(c) $x = -\frac{A}{4}$ (d) $x = 0$

Ans: 17. (b)

Q18. A point charge q is located at the apex of a cone of height h and base radius h . The flux of the electric field through the cone due to the point charge is



- (a) $\left(1 - \frac{1}{\sqrt{2}}\right) \frac{q}{2\pi\epsilon_0}$ (b) $\left(1 - \frac{1}{\sqrt{2}}\right) \frac{\pi q}{2\epsilon_0}$
(c) $\frac{1}{\sqrt{2}} \frac{q}{2\epsilon_0}$ (d) $\left(1 - \frac{1}{\sqrt{2}}\right) \frac{q}{2\epsilon_0}$

Ans: 18. (d)

Q19. Which of the following vanishes identically?

- (a) $\vec{\nabla} \times \frac{((y+x)\hat{i} + (y-x)\hat{j})}{x^2 + y^2}$ (b) $\vec{\nabla} \times \frac{(y\hat{i} - x\hat{j})}{x^2 + y^2}$
- (c) $\vec{\nabla} \times \frac{(x\hat{i} + y\hat{j})}{x^2 + y^2}$ (d) $\vec{\nabla} \cdot \left[\frac{(x\hat{i} + y\hat{j} + z\hat{k})}{(x^2 + y^2 + z^2)^{3/2}} \right]$

Ans: 19. (c)

Q20. Consider a two-level quantum system described by the Hamiltonian:

$$H = H_0 + H'$$

where

$$H_0 = \alpha \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} + \omega \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}, \quad H' = \epsilon \Gamma \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

H' is a small perturbation to the free Hamiltonian H_0 . ϵ is a small positive dimensionless number, while α, ω and Γ have dimensions of energy and are positive quantities. If we treat this problem perturbatively in the parameter ϵ , which of the following statements about the corrections to ground state energy is true?

- (a) First-order correction is $\epsilon \Gamma$; second-order correction is $-\frac{\epsilon^2 \Gamma^2}{2\omega}$
- (b) First-order correction is $\epsilon \Gamma$; second-order correction is 0.
- (c) First-order correction is 0; second-order correction is $-\frac{\epsilon^2 \Gamma^2}{2\omega}$
- (d) First-order correction is 0; second-order correction is $\frac{\epsilon^2 \Gamma^2}{2\omega}$

Ans: 20. (c)

Q 21 has been cancelled due to typographical error.

Q21. The spatial part of a two-electron state is anti-symmetric under exchange. If $|\uparrow\rangle$ and $|\downarrow\rangle$ represent the spin-up and the spin-down states respectively of each electron, the spin part of the two-electron state cannot be:

- (a) $\frac{1}{\sqrt{2}} (|\uparrow\rangle|\downarrow\rangle + |\uparrow\rangle|\downarrow\rangle)$ (b) $|\uparrow\rangle|\uparrow\rangle$
- (c) $\frac{1}{\sqrt{2}} (|\uparrow\rangle|\downarrow\rangle - |\uparrow\rangle|\downarrow\rangle)$ (d) $|\downarrow\rangle|\downarrow\rangle$

Ans: 21. (c)

Q22. How many independent real parameters are required to describe an arbitrary $N \times N$ Hermitian matrix?

- (a) $N^2 - N$ (b) N^2
(c) $2N$ (d) $N^2 - 1$

Ans: 22. (b)

Q23. Two fair six-faced dice are thrown simultaneously. The probability that one of the dice yields an outcome that is a multiple of 2 and the other yields a multiple of 3 is:

- (a) $\frac{1}{6}$ (b) $\frac{1}{3}$
(c) $\frac{13}{36}$ (d) $\frac{11}{36}$

Ans: 23. (d)

Q24. Convert the octal number 3720_8 to its decimal equivalent.

- (a) 1000_{10} (b) 2000_{10}
(c) 2020_{10} (d) 1900_{10}

Ans: 24. (b)

Q25. A steam engine takes steam from a boiler at 200°C (pressure 1.5×10^6 Pa) and exhausts directly into the air at 100°C (pressure 10^5 Pa). The maximum possible efficiency is closest to:

- (a) 78% (b) 21%
(c) 50% (d) 93%

Ans: 25. (b)

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Section B

Correct answer: +9, wrong answer: -3.

Q26. A gas is in equilibrium at temperature T . Using the kinetic theory of gasses, compute the following quantity:

$$\frac{\langle |\vec{v}| \rangle^2}{\langle |v_x| \rangle^2 + \langle |v_y| \rangle^2 + \langle |v_z| \rangle^2}$$

where \vec{v} represents the velocity vector with the components v_x, v_y, v_z and $\langle \dots \rangle$ represents the thermal average of the quantity.

- (a) 0 (b) $\frac{4}{3}$
(c) 1 (d) $\frac{1}{3}$

Ans: 26. (b)

Q27. Using the first law of thermodynamics $dU = TdS - PdV$, and the definitions of the thermodynamic potentials $H = U + PV, F = U - TS, G = H - TS$, work out the four Maxwell relations. Using these compute:

$$\chi = \left(\frac{\partial T}{\partial V} \right)_S + \left(\frac{\partial T}{\partial P} \right)_S + \left(\frac{\partial P}{\partial T} \right)_V + \left(\frac{\partial V}{\partial T} \right)_P$$

Which of the following does χ equal?

- (a) $\left(\frac{\partial S}{\partial V} \right)_T - \left(\frac{\partial S}{\partial P} \right)_T + \left(\frac{\partial V}{\partial S} \right)_P - \left(\frac{\partial P}{\partial S} \right)_V$ (b) $\left(\frac{\partial S}{\partial V} \right)_T - \left(\frac{\partial S}{\partial P} \right)_T + \left(\frac{\partial V}{\partial S} \right)_P + \left(\frac{\partial P}{\partial S} \right)_V$
(c) $\left(\frac{\partial S}{\partial V} \right)_T + \left(\frac{\partial S}{\partial P} \right)_T + \left(\frac{\partial V}{\partial S} \right)_P - \left(\frac{\partial P}{\partial S} \right)_V$ (d) $\left(\frac{\partial S}{\partial V} \right)_T + \left(\frac{\partial S}{\partial P} \right)_T + \left(\frac{\partial V}{\partial S} \right)_P + \left(\frac{\partial P}{\partial S} \right)_V$

Ans: 27. (a)

Q28. Compute the contour integral:

$$I = \oint \frac{zdz}{\sinh(2\pi z)}$$

where the contour is a circle of radius $\frac{3}{4}$ centred around the origin and the direction is counterclockwise.

- (a) 0 (b) -1
(c) π (d) 1

Ans: 28. (a)

Q29. Solve the differential equation,

$$\frac{dy}{dx} = xy + xy^2$$

If $y(x = \sqrt{2}) = \frac{e}{2-e}$ where e is the base of natural logarithms, compute $y(x = 0)$

- (a) -1 (b) 1
(c) e (d) 0

Ans: 29. (b)

Q30. One mole of an isolated ideal gas in equilibrium at pressure P_1 , volume V_1 , and temperature T_1 undergoes a process that changes its state. In the final state the gas is in equilibrium at pressure P_2 , volume V_2 , and temperature T_2 . Suppose the ratios of the final and initial temperatures and pressures are:

$$\eta_T = \frac{T_2}{T_1}, \quad \eta_P = \frac{P_2}{P_1}$$

Work out the change in entropy ΔS in the process. Take the heat capacities of the gas at constant pressure and constant volume to be C_p and C_v respectively, and the ideal gas constant to be R .

- (a) $C_p \ln(\eta_T) - R \ln(\eta_P)$ (b) $C_p \ln(\eta_T) + R \ln(\eta_P)$
(c) $C_v \ln(\eta_T) - R \ln(\eta_P)$ (d) $C_v \ln(\eta_T) + R \ln(\eta_P)$

Ans: 30. (a)

Q31. Two linear polarizers are placed coaxially with the transmission axis of the first polarizer in the vertical orientation and the second polarizer in the horizontal orientation. A half waveplate placed coaxially between these crossed polarizers is rotating about its axis at an angular frequency ω . At $t = 0$, the fast axis of the half waveplate was oriented vertically. A beam of unpolarized light of intensity I_0 is incident along the axis of this optical system. The output intensity measured by a detector after the beam passes through this optical system is

- (a) $\frac{I_0}{4} [1 + \cos(\omega t)]$ (b) $\frac{I_0}{4} [1 - \cos(2\omega t)]$
(c) $\frac{I_0}{4} [1 - \cos(4\omega t)]$ (d) $\frac{I_0}{2} [1 - \cos(\omega t)]$

Ans: 31. (c)

Q32. A particle of mass 1 kg, angular momentum $L = \sqrt{2} \text{ kg m}^2/\text{s}$ and total energy $E = 3 \text{ J}$ is subjected to a central force field $\vec{F} = -k\vec{r}$ where $k = 2 \text{ kg/s}^2$. Which of the following statements is true? [Note: The centres of all the circles in the options below are at the origin.] =

(a) The particle is constrained to be in the region outside the circle with radius $R = \sqrt{\frac{3+\sqrt{5}}{2}}$

(b) The particle is bounded within the annular region described by the two circles with radii $r_1 = \sqrt{\frac{5-\sqrt{3}}{2}}$ and $r_2 = \sqrt{\frac{5+\sqrt{3}}{2}}$.

(c) The particle is bounded within the annular region described by the two circles with radii $r_1 = \sqrt{\frac{3-\sqrt{5}}{2}}$ and $r_2 = \sqrt{\frac{3+\sqrt{5}}{2}}$.

(d) The particle is constrained to be in the region outside the circle with radius $R = \sqrt{\frac{5+\sqrt{3}}{2}}$.

Ans: 32. (c)

Q33. If a power series $y = \sum_{j=0}^{\infty} a_j x^j$ analysis is carried out of the following differential equation

$$\frac{d^2 y}{dx^2} + \frac{1}{x^2} \frac{dy}{dx} - \frac{4}{x^2} y = 0$$

which of the following recurrence relations results?

(a) $a_{j+1} = a_j \frac{4-j(j+1)}{j+1}$, $j = 0, 1, 2, \dots$ (b) $a_{j+2} = a_j \frac{4-j(j-1)}{j+1}$, $j = 0, 1, 2, \dots$

(c) $a_{j+2} = a_j \frac{4-j(j+1)}{j+1}$, $j = 0, 1, 2, \dots$ (d) $a_{j+1} = a_j \frac{4-j(j-1)}{j+1}$, $j = 0, 1, 2, \dots$

Ans: 33. (d)

Q34. Two semi-infinite wires are placed on the x - axis, one from $-\infty$ to the $-d$, and the other from d to ∞ . Both wires carry a steady current I in the same direction. The magnitude of the magnetic field at a distance d away from the center of this gap in the $y-z$ plane (ignore the charge accumulation) is:

(a) $\frac{\mu_0 I}{\pi d} \sqrt{2}$ (b) $\frac{\mu_0 I}{2\pi d} \left(1 - \frac{1}{\sqrt{2}}\right)$

(c) $\frac{\mu_0 I}{\pi d} \frac{1}{\sqrt{2}}$ (d) $\frac{\mu_0 I}{\pi d} \frac{1}{2}$

Ans: 34. (b)

Q38. Consider a quantum particle incident from the left on a step potential given by $V_0\theta(x)$, with energy $E(>V_0)$; here $\theta(x)$ is the unit step function. The scattering state of the particle is given by

$$\psi(x) = \begin{cases} \exp\frac{ipx}{\hbar} + r\exp\frac{-ipx}{\hbar}, & x < 0 \\ t\exp\frac{ip'x}{\hbar} & x > 0 \end{cases}$$

where p and p' are the momenta of the particle corresponding to the energy E . Which of the following is true?

- (a) $|r|^2 + \frac{p'}{p}|t|^2 = 1$ (b) $|r|^2 + |t|^2 = 1$
(c) $|r|^2 + \frac{p}{p'}|t|^2 = 1$ (d) $r+t=1$

Ans: 38. (a)

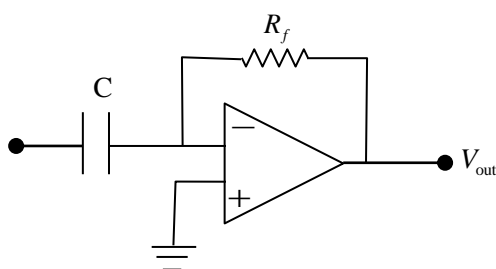
Q39. Consider a spin-1 system whose \hat{S}_z eigenstates are given by $| -1 \rangle, | 0 \rangle, | +1 \rangle$ corresponding to the eigenvalues $-\hbar, 0, \hbar$. The normalized general state $|\psi\rangle$ of the system can be expressed as $|\psi\rangle = c_{-1}| -1 \rangle + c_0| 0 \rangle + c_{+1}| +1 \rangle$ and c_{-1}, c_0, c_{+1} are complex numbers. Subjected to the condition $\langle \psi | \hat{S}_z | \psi \rangle = 0$, which of the following statements is true?

- (a) $|c_{+1}|^2 + 2|c_0|^2 = 1$ (b) $|c_{-1}|^2 + 2|c_0|^2 = 1$
(c) $2|c_{-1}|^2 + |c_{+1}|^2 = 1$ (d) $2|c_{-1}|^2 + |c_0|^2 = 1$

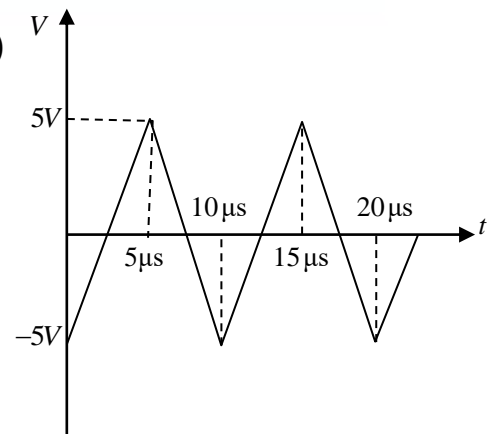
Ans: 39. (d)

Q40. Consider the Op-Amp differentiator presented in Figure (a). Take $C = 0.002\mu F$ and $R_f = 2k\Omega$. For a triangular wave input shown in the figure (b),

(a)

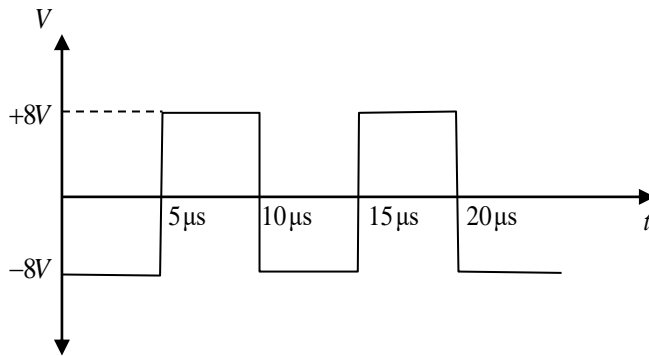


(b)

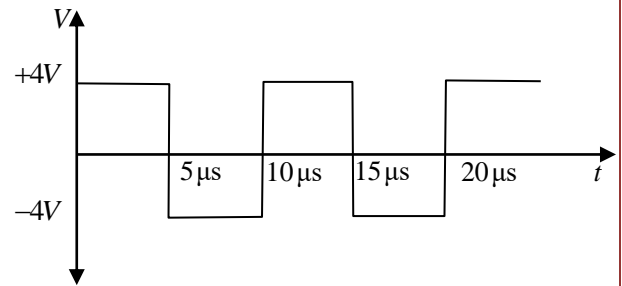


determine the output voltage waveform.

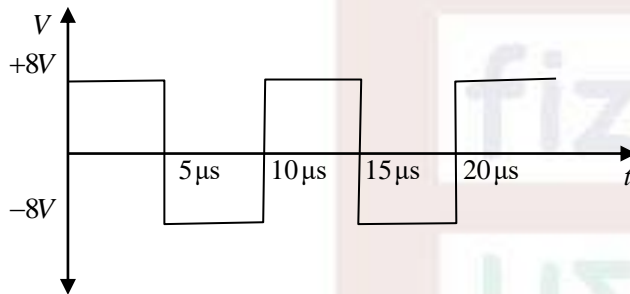
(a)



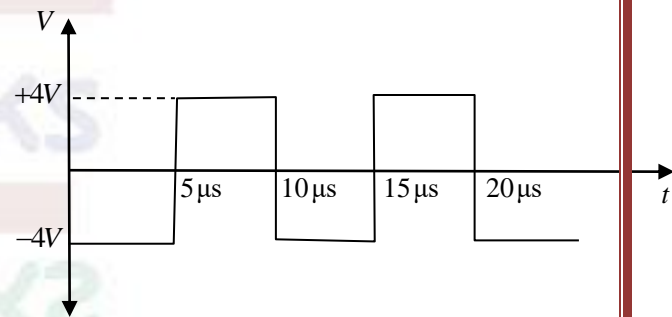
(b)



(c)

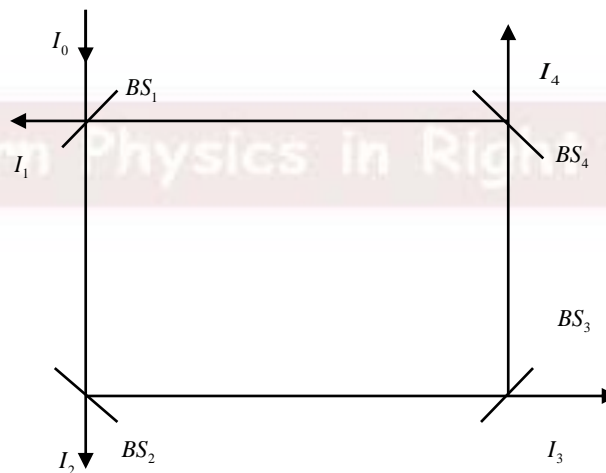


(d)



Ans: 40. (a)

Q41. A beam of light of intensity $I_0 = 120 \text{ W/m}^2$ is incident on the optical system shown in the figure. $BS_1, BS_2, BS_3,$ and BS_4 are ideal, 50/50 beamsplitters (reflects 50% and transmits 50% of incident light intensity). $I_1, I_2, I_3,$ and I_4 are the total intensities measured by detectors. What will be the intensity I_3 ?



(a) 32 W/m^2

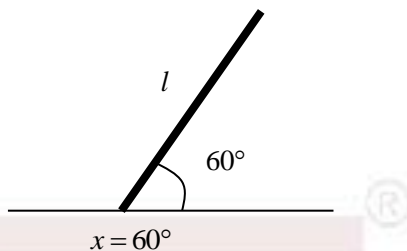
(b) 20 W/m^2

(c) 16 W/m^2

(d) 12 W/m^2

Ans: 41. (c)

Q42. A rod of length $l=1$ meter is held on a frictionless horizontal surface at an angle of $\theta = 60^\circ$ with the horizontal, as shown in the figure. Take the point of contact of the rod with the horizontal plane as the origin ($x=0$). As the support holding the rod is suddenly removed, the rod comes in contact with the horizontal surface. What will be the coordinate of the left end of the rod at the moment of contact?



- (a) -0.15 m (b) -0.5 m
(c) -0.2 m (d) -0.25 m

Ans: 42. (d)

Q43. Consider a particle subjected to the symmetric one-dimensional infinite square well potential:

$$V(x) = \begin{cases} 0, & |x| \leq \frac{L}{2} \\ \infty, & |x| > \frac{L}{2} \end{cases}$$

Find the time evolution of the wavefunction $\psi(x,t)$, if at time $t=0$ the particle is prepared in an equal superposition of the ground and the first excited states:

$$\psi(x,0) = \frac{1}{\sqrt{2}}(\phi_1(x) + \phi_2(x))$$

where $\phi_1(x)$ and $\phi_2(x)$ are normalized eigenfunctions of the ground state and the first excited state respectively. If τ is the smallest time at which the particle is equally likely to be in either half of the well, select the correct value of $\frac{\tau h}{mL^2}$,

where h is the Planck's constant, m is the mass of the particle and L is the width of the well as defined above.

- (a) $\frac{2}{3}$ (b) $\frac{1}{3}$
(c) $\frac{1}{6}$ (d) $\frac{4}{3}$

Ans: 43. (a)

Q44. A conducting spherical soap bubble of radius R with a wall thickness of W ($\ll R$) is charged to a potential of V_0 . The bubble bursts and becomes a spherical drop with potential V_d .

Select the correct value of the ratio $\eta = \frac{V_d^3 W}{V_0^3 R}$

- (a) $\frac{1}{3}$ (b) $\frac{1}{6}$
(c) $\frac{1}{4}$ (d) $\frac{2}{3}$

Ans: 44. (a)

Q45. Consider the operator $\vec{S} \cdot \hat{n}$ with eigenkets $|\pm\rangle_{\hat{n}}$ and eigenvalues $\pm \frac{\hbar}{2}$ where \hat{n} is a unit vector and \vec{S} is the spin operator. A partially polarized beam of spin- $\frac{1}{2}$ particles contains a 25-75 mixture of two pure ensembles, one with $|+\rangle_z$ and the other with $|+\rangle_x$ respectively. What is the ensemble average of $\frac{\vec{S} \cdot \hat{x}}{\hbar}$?

- (a) $\frac{1}{3}$ (b) $\frac{3}{8}$ (c) $\frac{1}{4}$ (d) $\frac{3}{16}$

Ans: 45. (b)

Q46. Given the vector $\vec{v} = y\hat{i} + 3x\hat{j}$, what is the value of the line integral $\oint \vec{v} \cdot d\vec{r}$ along the unit circle (centered at the origin) in an anti-clockwise direction?

- (a) $\frac{2\pi}{3}$ (b) π
(c) 0 (d) 2π

Ans: 46. (d)

Q47. Choose the largest eigenvalue of the matrix

$$\begin{pmatrix} 1 & 1 & 1 & 2 & 3 \\ 12 & 2 & 3 & 2 & 1 \\ 0 & 0 & 0 & 2 & 2 \\ 0 & 0 & 3 & 0 & 3 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

- (a) 3 (b) 5
(c) 8 (d) 10

Ans: 47. (b)

Q48. A cylinder of height L and cross-section A placed vertically along the central axis is filled with non-interacting particles each of mass m which are acted upon by a gravitational force of magnitude mg in the downward direction. The system is maintained at a temperature T . What is the ratio $\frac{C_v(T \rightarrow 0)}{C_v(T \rightarrow \infty)}$, where C_v is the specific heat at constant volume.

- (a) $\frac{3}{5}$ (b) $\frac{3}{2}$
(c) $\frac{1}{3}$ (d) $\frac{5}{3}$

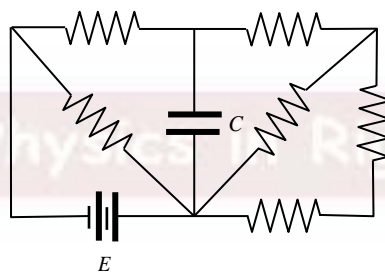
Ans: 48. (d)

Q49. System A consists of 3 identical non-interacting bosons. System B consists of 2 identical non-interacting bosons. They both have identical energy spectra - three non-degenerate energy levels $0, \epsilon, 2\epsilon$. The particles of A and B are distributed in various energy levels in such a way that the total energy of the combined system is 4ϵ . The average energy of the system A in units of ϵ is

- (a) 2.2 (b) 2.3
(c) 2.1 (d) 2.4

Ans: 49. (b)

Q50. Consider the circuit shown in the figure below. C is the capacitance of the capacitor, E is the voltage provided by the battery and all the resistors are identical. What is the charge stored in the capacitor in units of CE , once it is fully charged.



- (a) $\frac{3}{4}$ (b) $\frac{5}{8}$
(c) $\frac{3}{8}$ (d) $\frac{5}{4}$

Ans: 50. (b)

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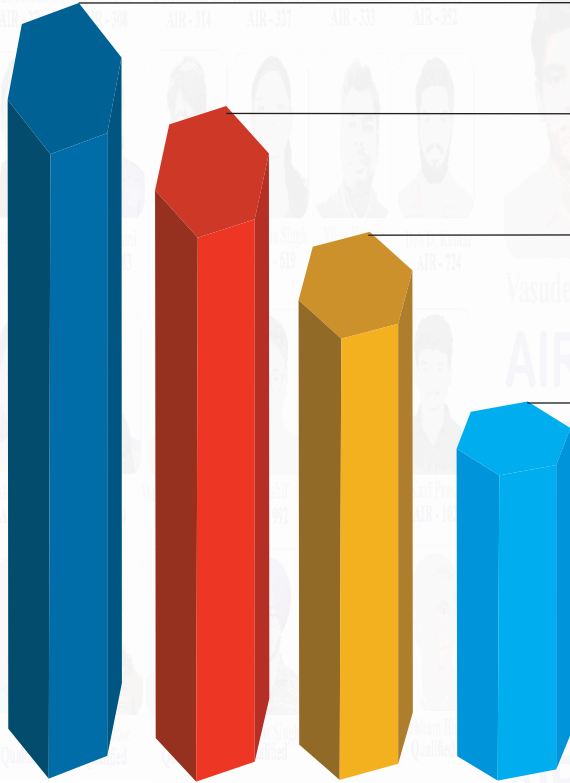


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